

# Residual-Based Measurement of Peer and Link Lifetimes in Gnutella Networks

**Xiaoming Wang**

Joint work with Zhongmei Yao and Dmitri Loguinov

Internet Research Lab  
Computer Science Department  
Texas A&M University

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# Agenda

- Introduction
- Related work
  - Create-Based Method (CBM)
- Analysis of CBM
- Proposed method
  - Residual-Based Estimator (RIDE)
- Comparison of overhead
- Experiments
- Conclusion

# Introduction

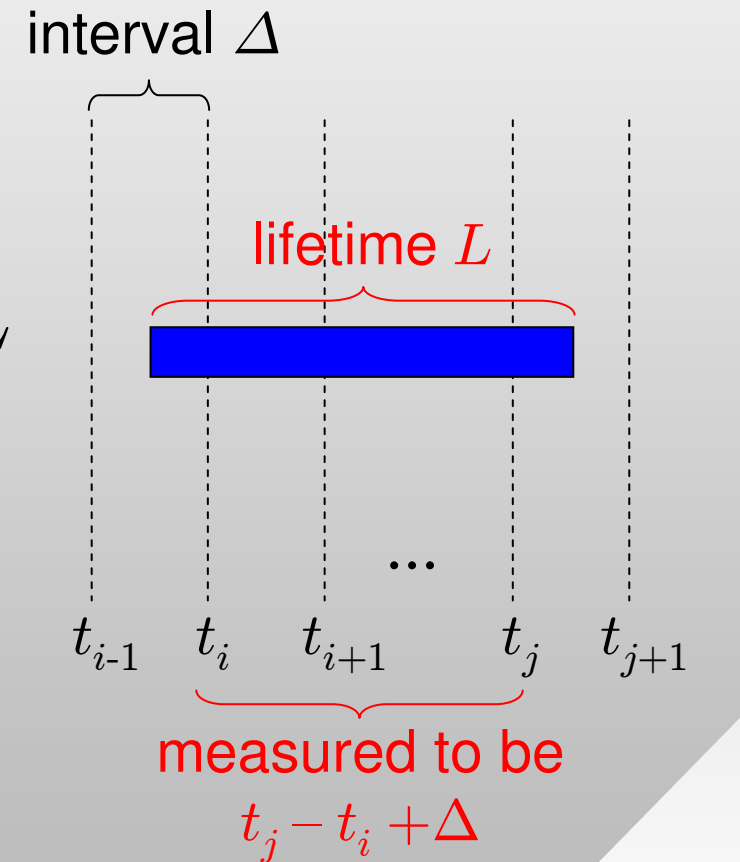
- Current peer-to-peer networks
    - Have a large number of participating users
    - Are organized in a decentralized infrastructure
  - Measurements are needed for validation purposes
    - Lifetime distribution
    - Inter-arrival delays
    - Availability
    - Topological information
    - Traffic flow rate
- our focus

# Introduction – Lifetime Sampling

- Measuring lifetime distribution
  - Collecting lifetime samples
- The lifetime of a user can be measured **only if one observes both its birth and death**
- To detect arrivals and departures, one must have periodic snapshots of the whole system

# Introduction – Lifetime Measurement

- Take snapshots of the system every  $\Delta$  time units
- Consider a user with lifetime  $L$ 
  - The user is captured in the snapshots taken at time points  $t_i, t_{i+1}, \dots, t_j$
  - Then, the measured lifetime of this user is rounded up to  $t_j - t_i + \Delta$
- Create-Based Method (CBM)



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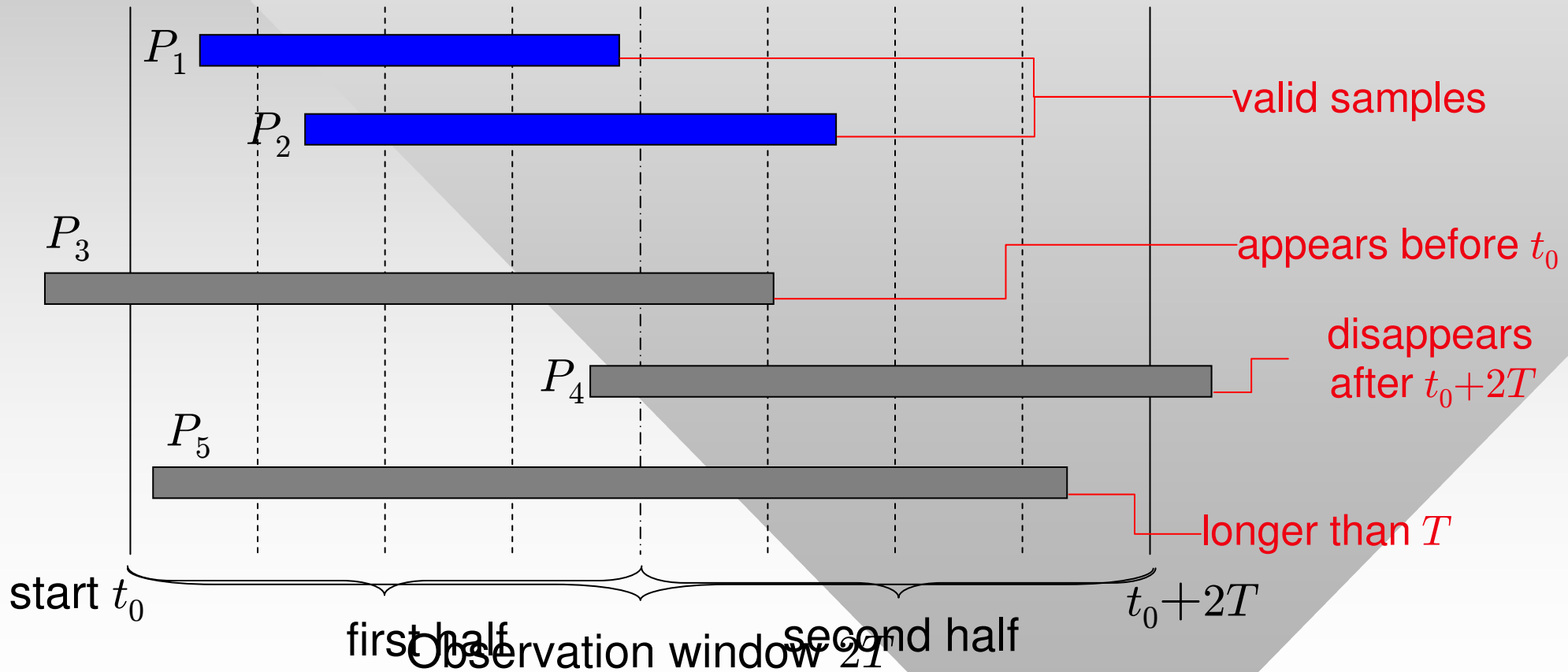
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# Related Work – CBM Sampling

1. Appear during the first half of the window

2. Disappear somewhere in the window

3. Stay in the system no longer than  $T$  time units



# Related Work – CBM Estimators

criteria of unbiased estimator

CDF function  $F(x)$

- Denote by  $E(x)$  the estimated value for the probability a random lifetime  $L$  is no larger than  $x$ 
  - We want  $E(x) = P(L \leq x) \equiv F(x)$  to hold for discrete points  $x = j\Delta, j = 0, 1, 2, \dots, T/\Delta$

- Two CBM estimators have been proposed
  - Roselli 2000

$$E_A(x_j) = \frac{N(x_j)}{N(T)}$$

$x_j = j\Delta$  — valid samples smaller than  $x_j$   
 $N(T)$  — total valid samples

- Saroiu 2002, Bustamante 2003, Stutzbach 2006

$$E_B(x_j) = \frac{N(x_j)}{N}$$

$N$  — total observed samples that appear in the first half window

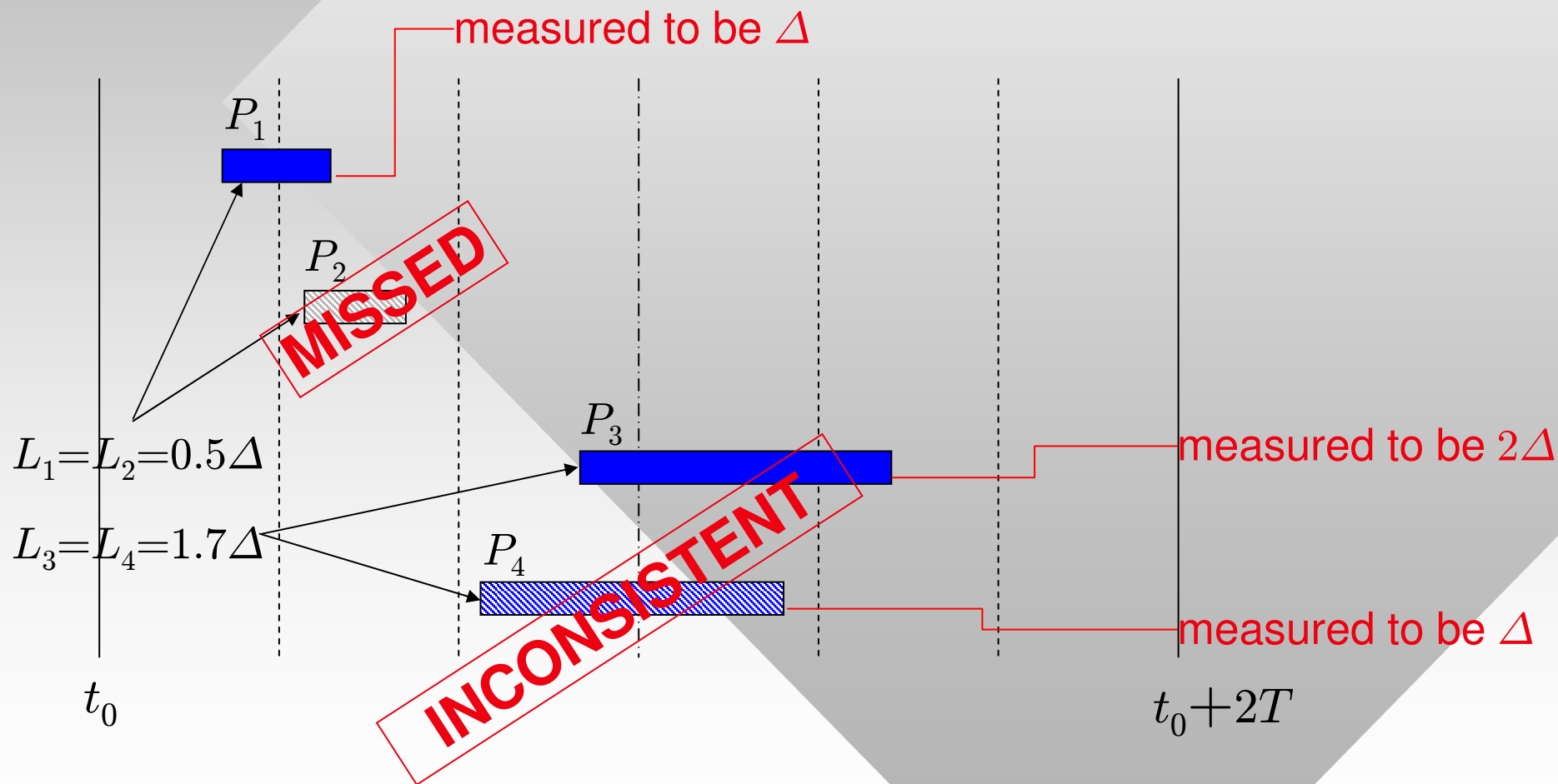


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# CBM – Round-off Errors

- Round-off errors may cause bias in CBM



# CBM – Model

- target  $P(L \leq x_j)$       probability of round-off errors      not affected by T more accurate
- Theorem 1: Both CBM estimators differ from the actual lifetime distribution as follows

$$E_A(x_j) = \frac{F(x_j) + \rho_j - \rho_0}{F(T) - \rho_0}$$

$$E_B(x_j) = \frac{F(x_j) - \rho_0 + \rho_j}{1 - \rho_0}$$

– where

probability  $P(L \leq T)$

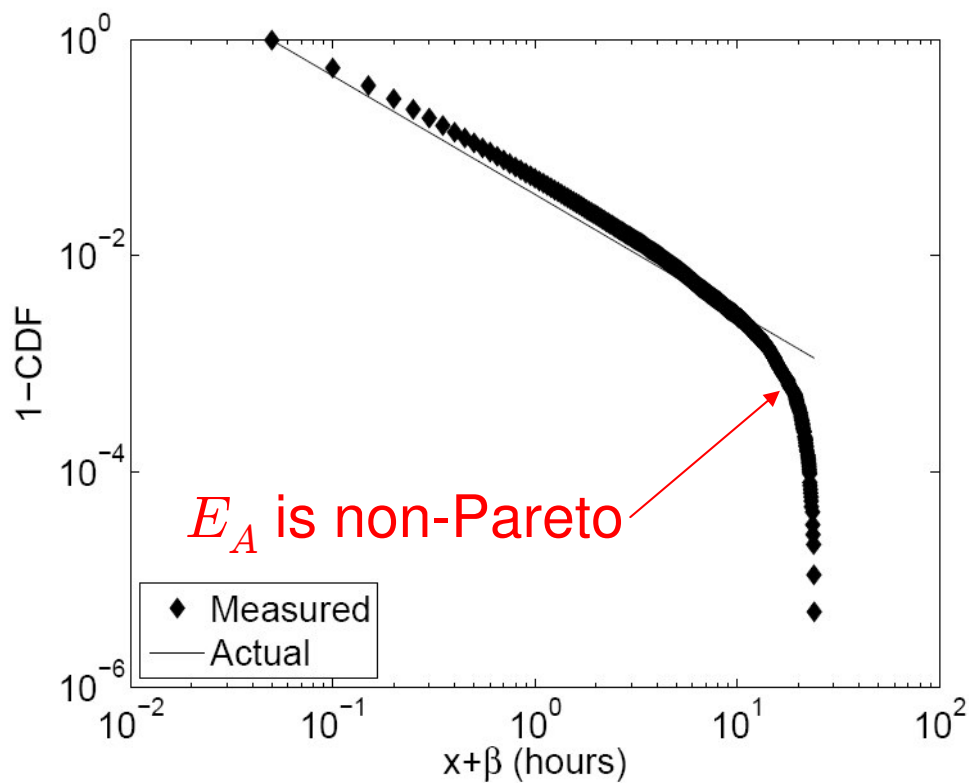
$$\rho_j = \frac{1}{\Delta} \int_0^{\Delta} F(x + x_j) dx - F(x_j)$$

- In fact, actual  $F(x)$  can be recovered from  $E_B$  **only** if  $\rho_j$  are known
  - However,  $\rho_j$  can be neither measured in practice nor calculated without knowing  $F(x)$
- Therefore,  $E_B$  as well as  $E_A$  are inherently biased

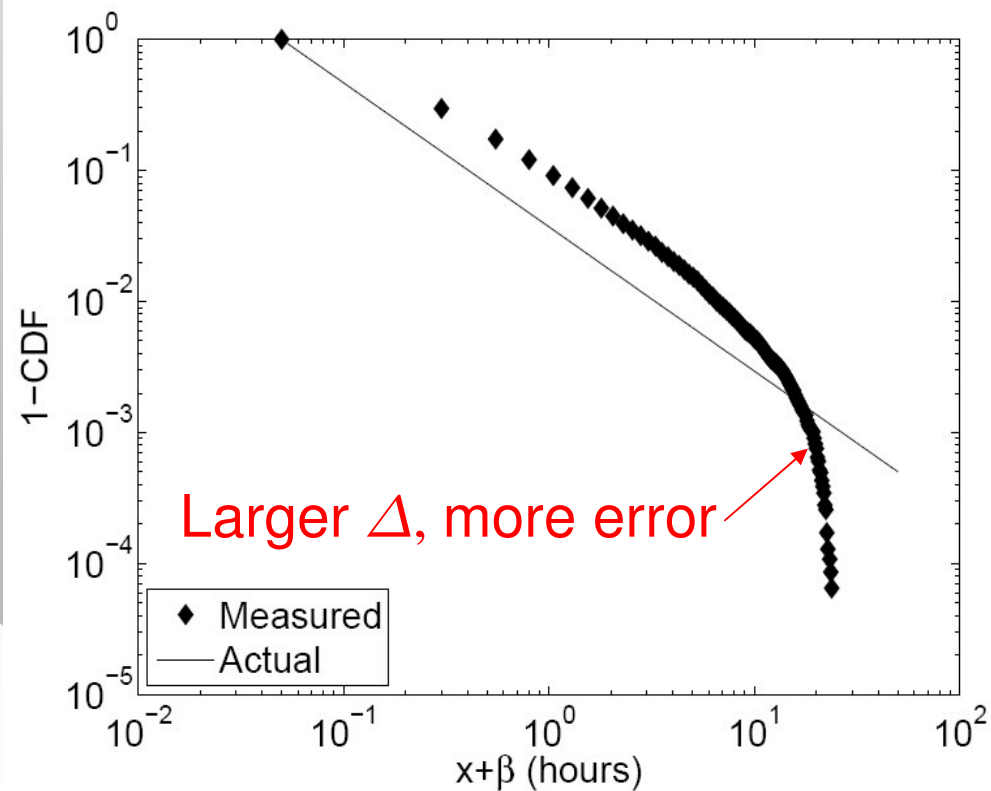
# CBM – Simulations with $E_A$

$$F(x) = 1 - (1 + x/\beta)^{-\alpha}$$

- Actual lifetimes follow a Pareto distribution
  - $\alpha=1.1$ ,  $\beta=0.05$ ,  $E[L]=0.5$  hours,  $T=24$  hours



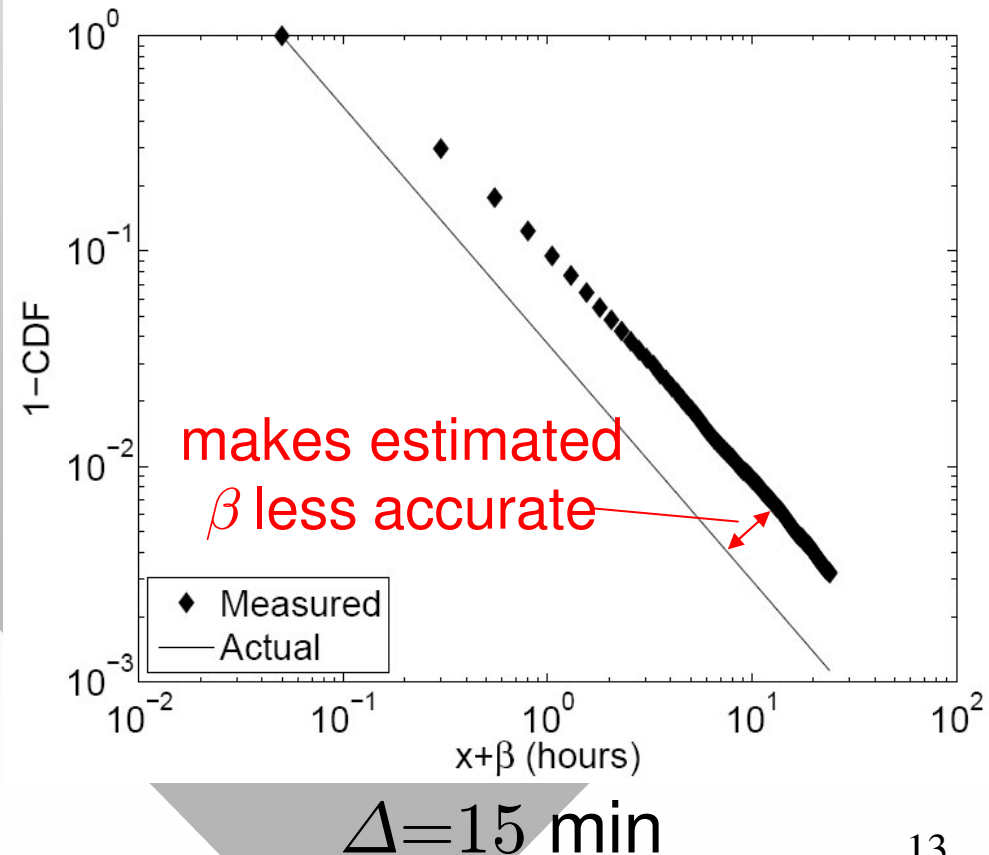
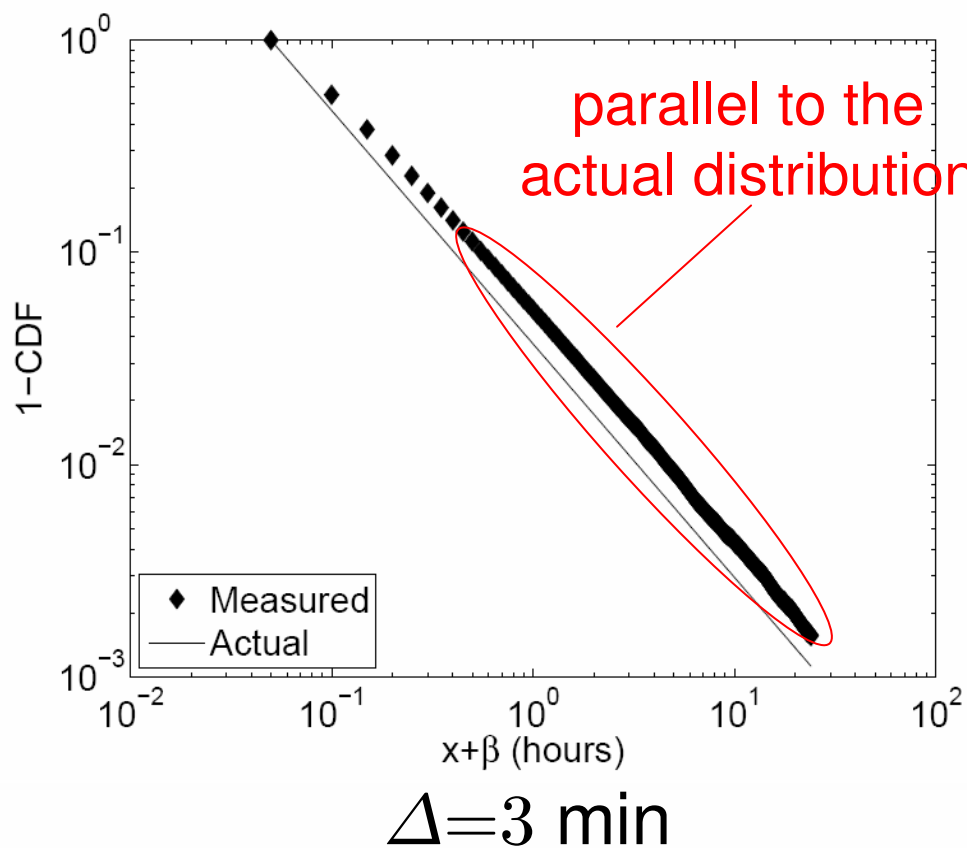
$\Delta=3$  min



$\Delta=15$  min

# CBM – Simulations with $E_B$

- Estimator  $E_B$  preserves the Pareto shape  $\alpha$  for small  $\rho_j$ 
  - But makes the Pareto scale  $\beta$  inaccurate



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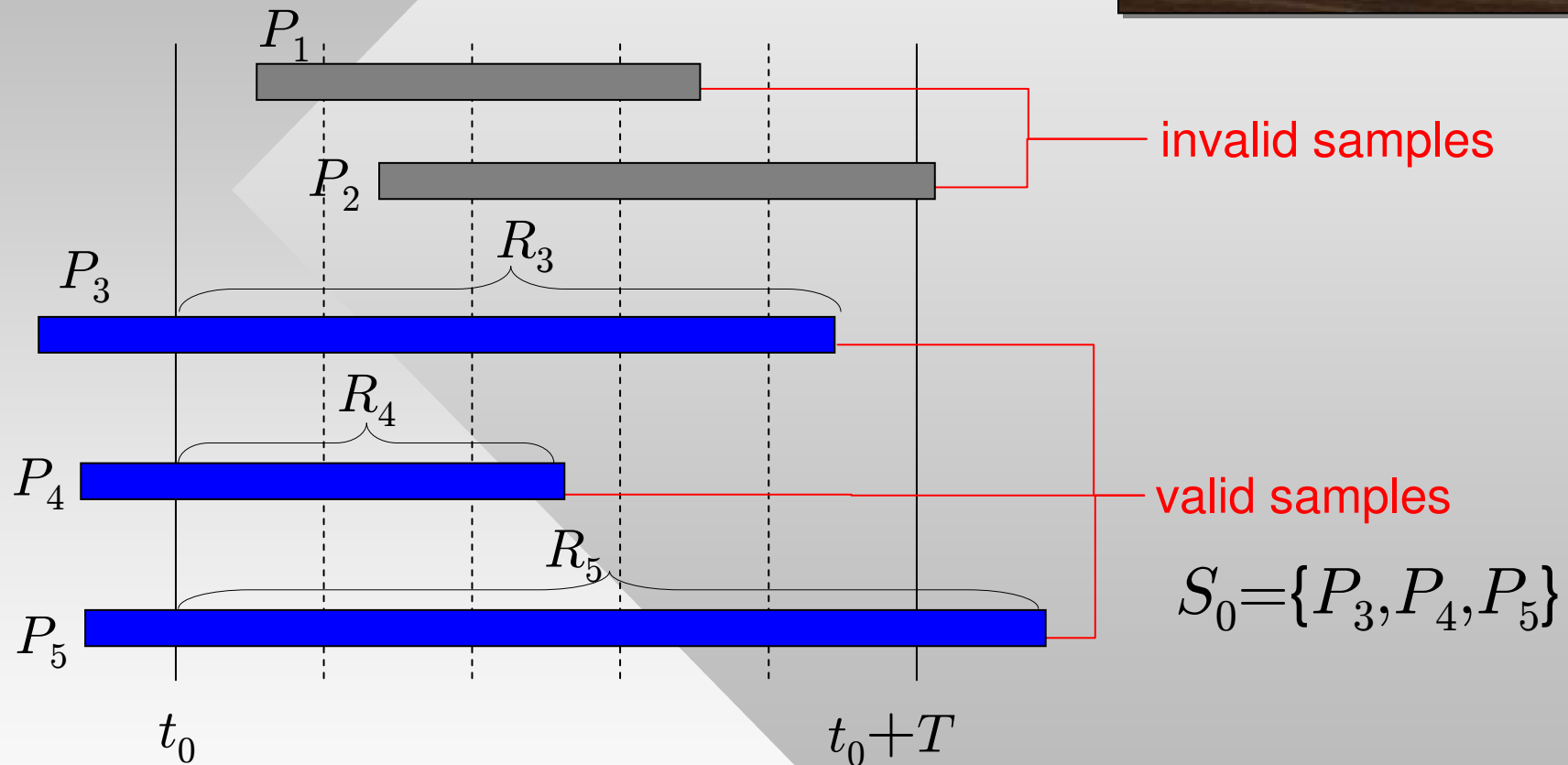
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# Residual-Based Method – Motivation

- Larger  $\Delta$  implies more bias in CBM
  - It is desirable to crawl the system as frequently as possible
- Smaller  $\Delta$  means more traffic overhead
  - Moreover,  $\Delta$  cannot be smaller than the time needed for crawling the entire system
- There is an inherent tradeoff between accuracy and overhead in CBM
- We propose **Residual-Based Estimator (RIDE)**

# RIDE – Sampling

1. Alive at the time of the first crawl



- RIDE samples the **residual lifetime**  $R$  of users in  $S_0$ 
  - From time  $t_0$  until the user dies



# RIDE – Subsampling

- RIDE acquires **all valid samples** in the initial set  $S_0$  during the very first crawl
  - This allows us to randomly subsample the users in set  $S_0$
- Suppose we track the residuals of only  $\epsilon$  **percent** of the entire initial set  $S_0$ 
  - Significantly reduce traffic requirements
- Note that subsampling is not possible in CBM
  - It requires **full system crawls** to discover new users

# RIDE – Estimator

- RIDE has all valid samples starting from  $t_0$ 
  - It will never miss any sample nor have any round-off errors
- Theorem 2: The following equation defines an unbiased estimator

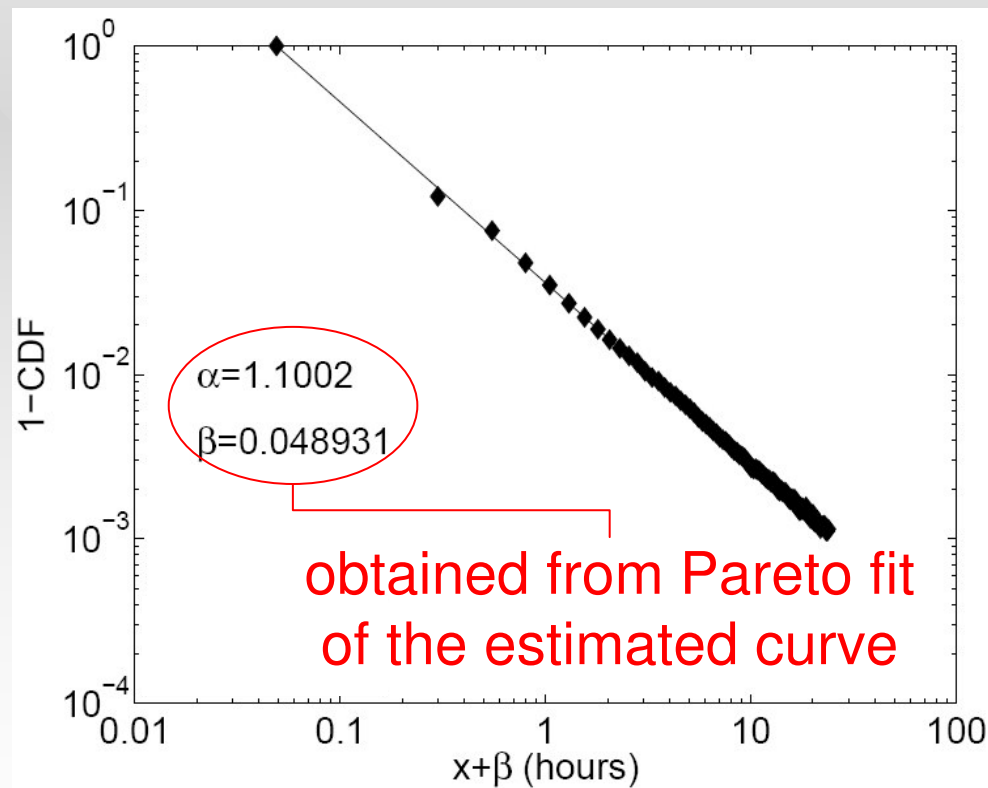
$$E_R(x_j) = 1 - \frac{h(x_j)}{h(0)}$$

estimated probability  $P(L \leq x_j)$

PDF of residuals lifetimes

# RIDE – Simulations without Subsampling

- Lifetimes are Pareto with  $\alpha=1.1$ ,  $\beta=0.05$ 
  - $E[L]=0.5$  hours,  $T=24$  hours,  $\Delta=15$  min,  $|S_0|=1M$

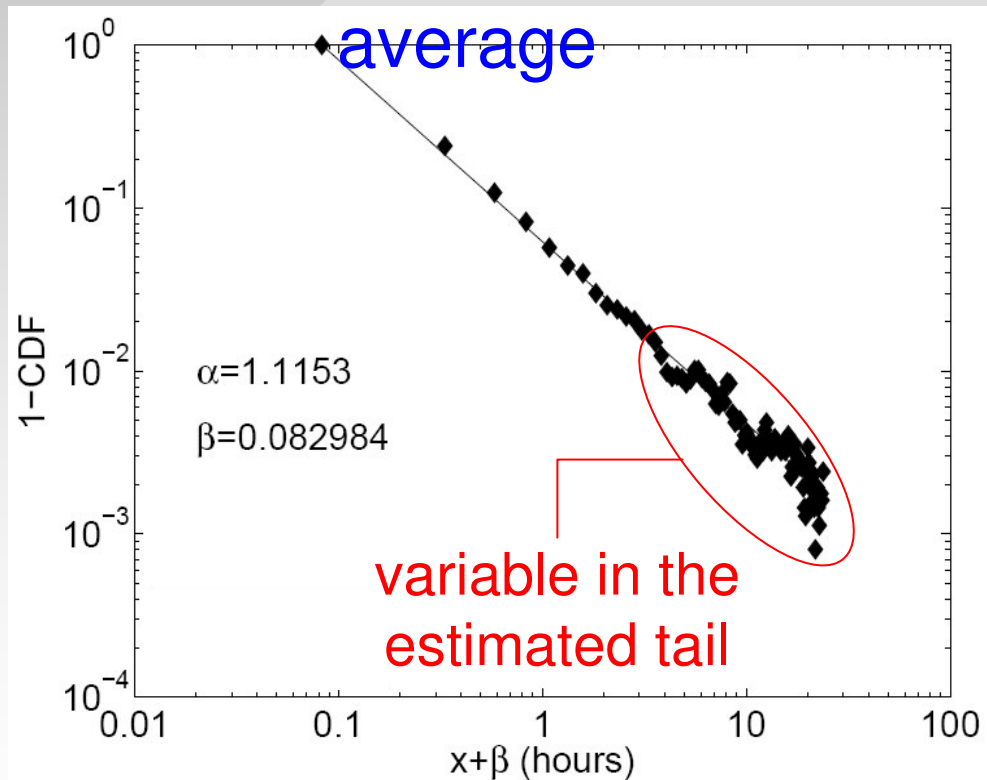


$$\epsilon=1$$

# RIDE – Simulations with Subsampling

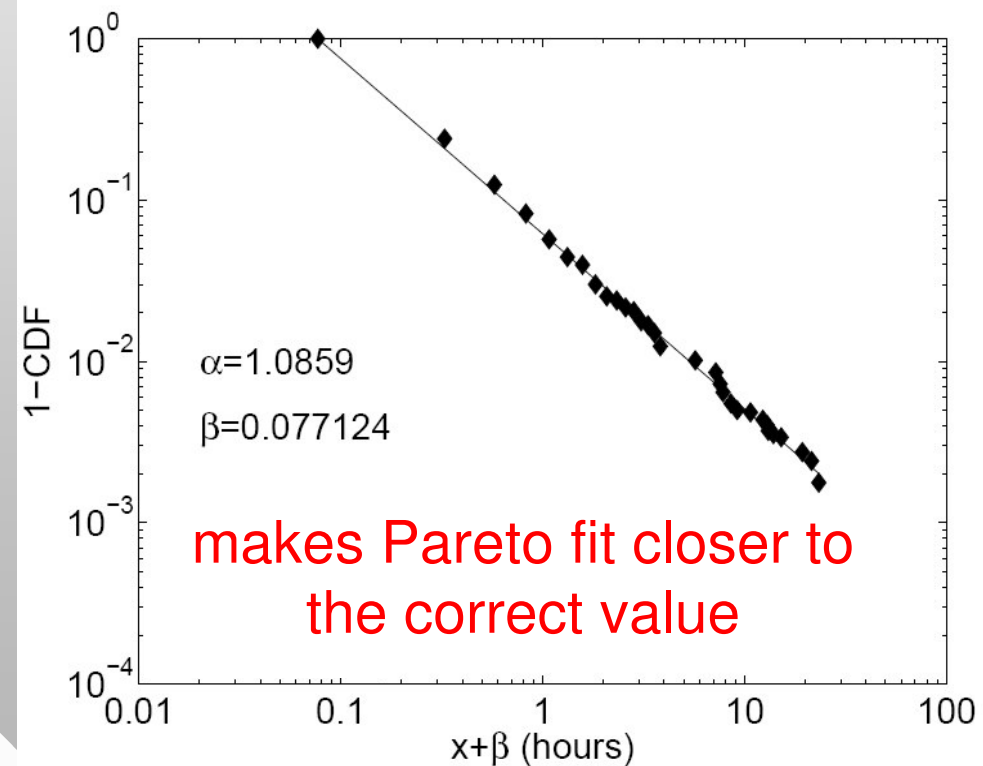
- Applying inverse average

before inverse average



$\epsilon=0.01$

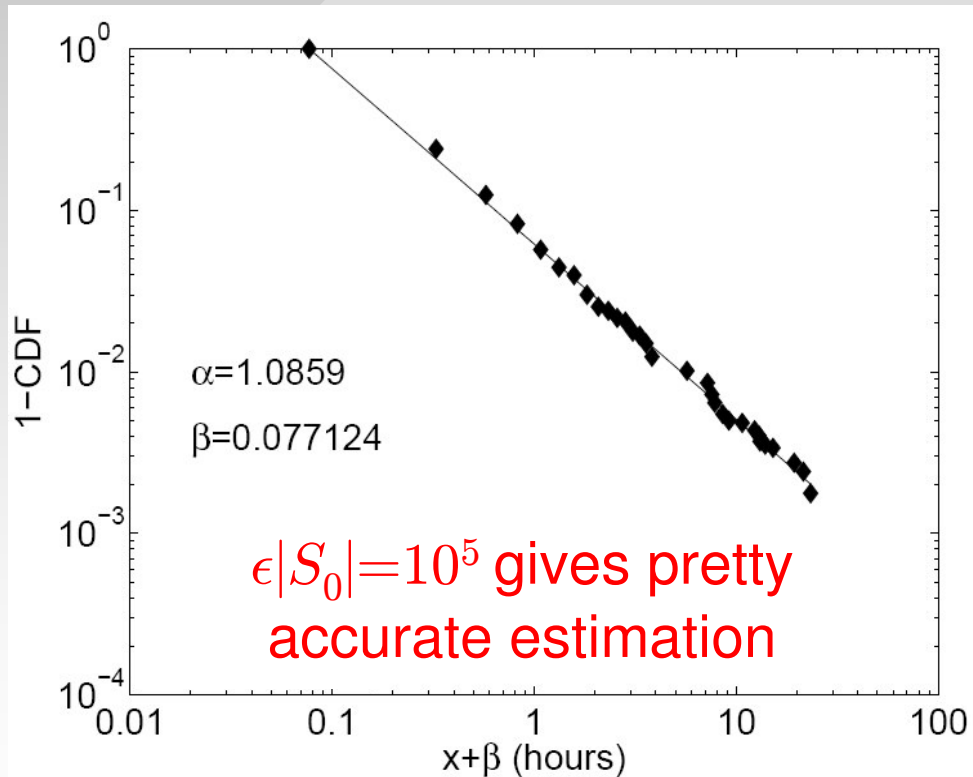
after inverse average



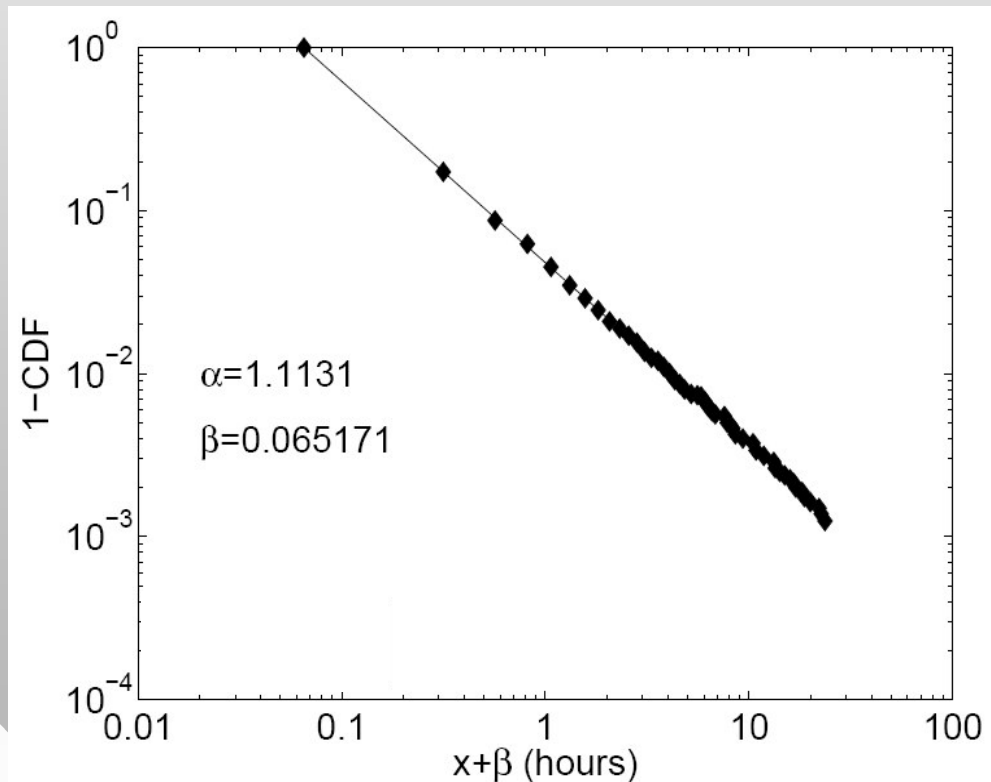
$\epsilon=0.01$

# RIDE – Simulations with Subsampling

- Applying inverse average



$\epsilon=0.01$



$\epsilon=0.1$

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# Overhead Comparison

- Theorem 3: Total bandwidth overhead of  $(\Delta, T)$ -sampling using CBM and RIDE is given by:

$$b_{CBM} = \frac{Cn}{\Delta} \left( T + \int_0^T [H(T) - H(x)] dx \right)$$

cost of  
crawling a user

users concurrently in  
the system

residual CDF

$$b_{RIDE} = \frac{C|S_0|}{\Delta} \left( \Delta + \epsilon \int_0^T [1 - H(x)] dx \right)$$

subsampling percentage

- Define  $q(\epsilon)$  the ratio of overhead of CBM and RIDE

$$q(\epsilon) = \frac{b_{CBM}}{b_{RIDE}}$$

## Overhead Comparison (cont.)

- Pareto lifetime with  $E[L]=1$  hours,  $\Delta=3$  min

$\alpha$	$T$	$q(0.1)$	$q(0.01)$
1.1	24 hrs	16	125
	48 hrs	17	151
	72 hrs	18	164

$\alpha$	$T$	$q(0.1)$	$q(0.01)$
2	24 hrs	71	319
	48 hrs	116	573
	72 hrs	157	811

smaller  $\epsilon$ ,  
more savings

larger  $T$ ,  
more savings

RIDE saves overhead  
by a fact of more than 800

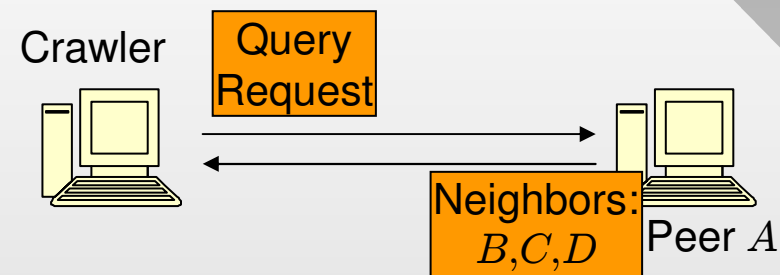
- In fact, we can choose proper  $\epsilon$  based on the size of the initial set  $S_0$ 
  - $\epsilon|S_0|$  is fixed at some pre-determined value, e.g.,  $10^5$

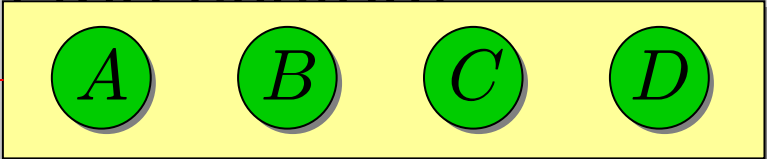
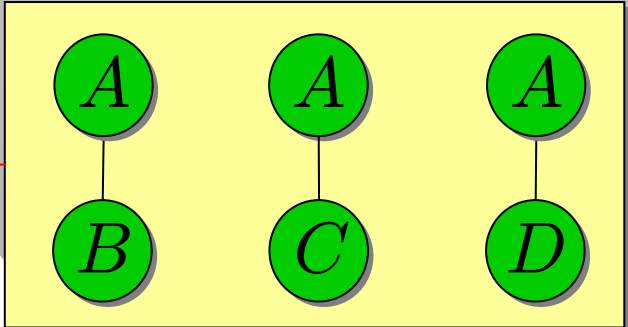


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# Experiments – Gnutella



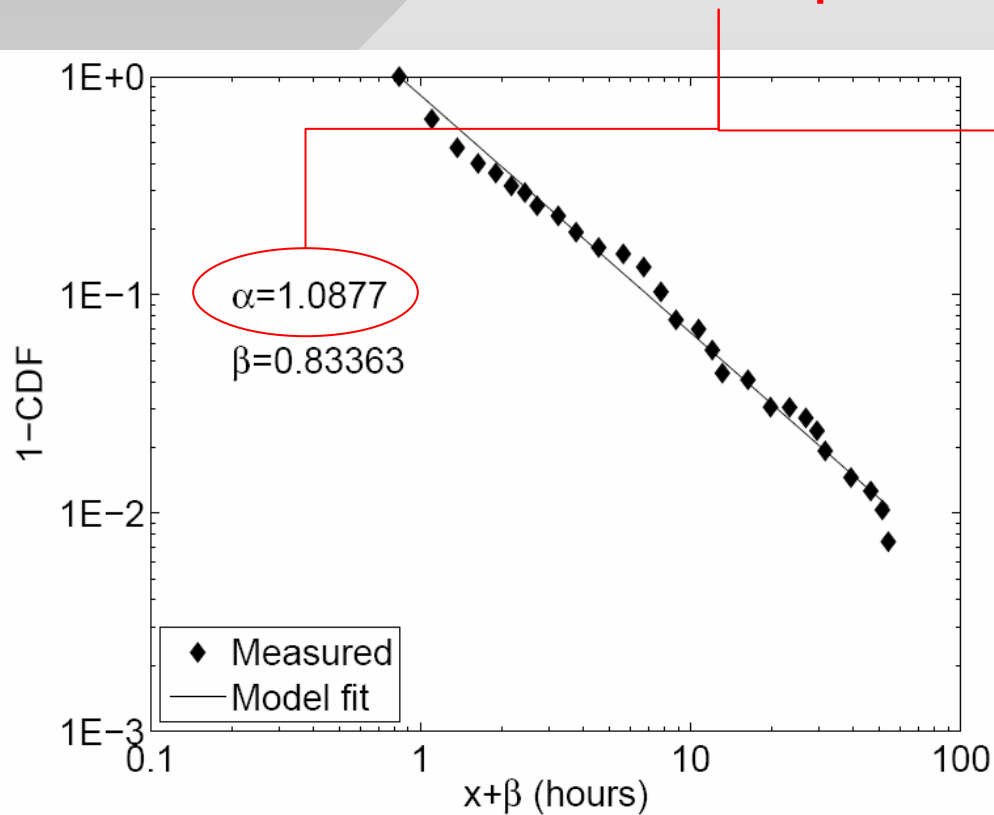
- Gnutella is fully distributed
  - However, it allows to query the neighbor list of any node
- Using Breadth-First-Search (BFS), we can take the snapshots of the users in the system
  - Peers  $A, B, C, D$  peer snapshot

- Moreover, we can infer link information from query replies
  - Links  $(A, B), (A, C), (A, D)$  link snapshot


# Experiments – Gnutella Crawler

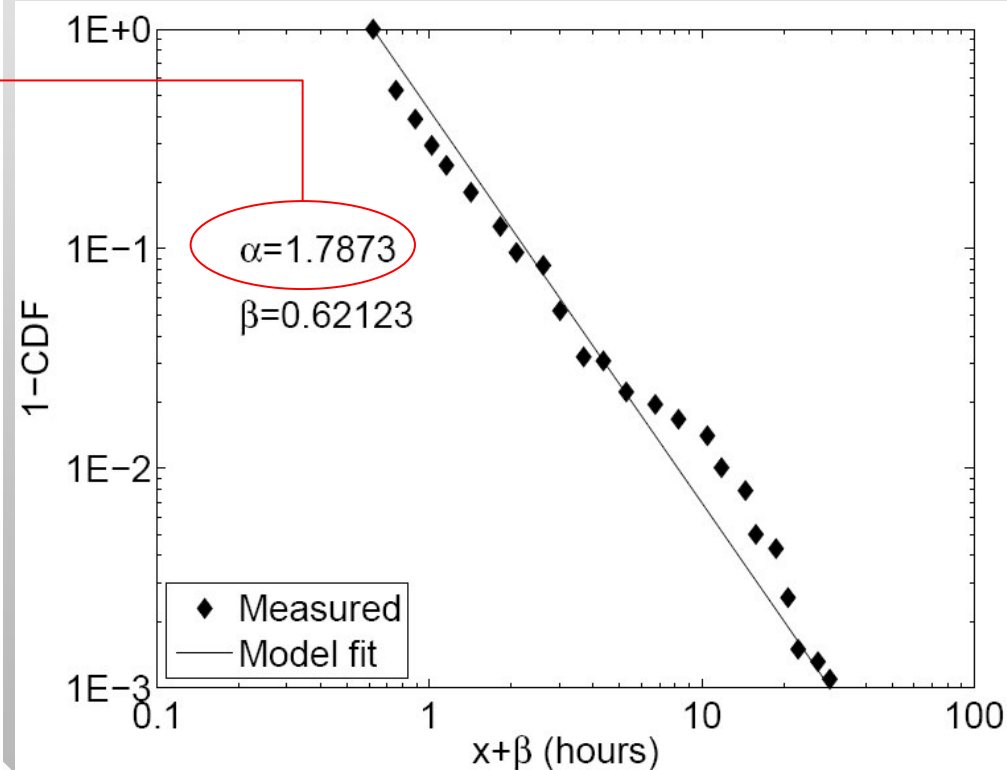
- We implemented a Gnutella crawler – **GnuSpider**
  - BFS search among ultra-peers
  - Up to 60,000 simultaneous connections
  - 216,000 contacted ultra-peers per min
- Entire system crawled in 3 min on July 22, 2006
  - 6.4 million users (1.2 million ultra and 5.2 million leaves)
- First crawl obtains 468,000 responsive ultra-peers
  - Subsampling  $\epsilon|S_0| = 100,000$
  - $\Delta=3$  min,  $T=72$  hours

# Experiments – Lifetime Distributions

Lifetimes are Pareto with very heavy-tailed  
 $\alpha \approx 1.09$  and  $1.8$  for ultrapeers and links



responsive  
ultrapeer



associated  
links

## Conclusion

- CBM is generally biased for  $\Delta > 0$ 
  - It may not scale to large networks
- RIDE can reduce traffic overhead by several orders of magnitude
  - Generally more accurate and scalable than CBM
- Ultrapeer lifetimes are Pareto with  $\alpha \approx 1.09$ 
  - $\alpha \approx 1.06$  (Bustamante 2003)
- Link lifetimes exhibit much lighter tails with  $\alpha \approx 1.8$ 
  - More volatile than ultrapeers